Total Pages : 05

Roll No.

(41)

D-C-190041

B. Tech. EXAMINATION, 2019

Semester IV (CBS)

OPTIMIZATION AND CALCULUS OF VARIATIONS

(CE, ME, AE, ECE, EE, EEE, CSE, IT)

MA-401

Time : 3 Hours

Maximum Marks : 60

The candidates shall limit their answers precisely within the answer-book (40 pages) issued to them and no supplementary/continuation sheet will be issued.

Note : Attempt *Five* questions in all, selecting *one* question from each Section A, B, C and D. Q. No. 9 is compulsory.

Section A

1. (a) Minimize Z = 6x + 14y; 6

subject to constraints
$$\begin{cases} 5x + 4y \ge 60; & 3x + 7y \le 84\\ x + 2y \ge 18; & x, y \ge 0 \end{cases}$$

by graphical method.

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- (b) Explain the following in the context of linear programming problem : 6
 - (i) Feasible solution
 - (ii) Objective function
 - (iii) Non-negativity constraints.
- 2. Use simplex method to solve the following linear programming problem : 12

Maximize $Z = 107x_1 + x_2 + 2x_3$; subject to constraints :

> $14x_1 + x_2 - 6x_3 + 3x_4 = 7$ $16x_1 + 0.5x_2 - 6x_3 \le 5$ $3x_1 - x_2 - x_3 \le 0$ $x_1, x_2, x_3, x_4 \ge 0.$

Section B

3. Solve the following Linear programming by the method of dynamic programming :

Maximize $Z = 50x_1 + 100x_2$, Subject to :

$$10x_1 + 5x_2 \le 2500$$

$$4x_1 + 10x_2 \le 2000$$

$$x_1 + 1.5x_2 \le 450$$

$$x_1, x_2 \ge 0.$$

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Find the optimum solution of the following transportation problem in which the cells contain the transportation cost in rupees : 12

	D	D ₂	D ₃	D ₄	Available
Α	11	13	17	14	250
В	16	18	14	10	300
С	21	24	13	10	400
Requirement 200		225	275	250	

Section C

- A project consists of the following activities with the 5. time estimates noted against each : 12 Activity Time estimates Activity Time estimates (weeks) (weeks) 5 2 3-7 1-2 4-6 3 1-3 2 5-8 1 1-4 1 6-9 5 4 2-5 7-8 8 4 3-6 8-9 3
 - (a) Draw a network diagram.
 - (b) Determine the critical path and its duration.
 - (c) Calculate the total float for each activity.

(a) Draw a n (b) Determine (c) Calculate (c) W-D-C-199941

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6. Consider the Non-linear Programming Problem : 12

Maximize $Z = 2x_1^2 - 24x_1 + 2x_2^2 - 8x_2 + 2x_3^2 - 12x_3 + 200$

By separating this function into three one-variable functions, show that the function is convex. Solve the problem by solving each one-variable function by calculus.

Section D

- 7. (a) Prove that the shortest distance between two points in a plane is a straight line. 6
 - (b) Find the extremal of the functional

 $I = \int_0^{\pi} \left[(y')^2 - y^2 + 4y \cos x \right] dx \quad \text{under} \quad \text{the}$

conditions
$$y(0) = 0, y(\pi) = 0$$
. 6

- 8. (a) Prove that the geodesics on a sphere of radius a are its great circles. 6
 - (b) Find the plane curve of fixed perimeter and maximum area. 6

Section E

(Compulsory Question)

- 9. Atempt all the parts : 1×1
 - (a) What is the essential difference between regular simplex method and dual simplex method ?

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1×12=12

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- (b) Explain the concept of duality in linear programming.
- (c) Write the number of non-negative variables in a
- basic feasible solution to a $m \times n$ transportation problem.
- (d) Define balanced transportation problem.
- (e) What is optimum basic feasible solution ?
- (f) Define Slack variable in the context of Linear Programming Problems.
- (g) Write two applications of network model.
- (h) Define degeneracy of transportation problem.
- (i) What is the expected time for PERT calculations?
- (i) Write the statement of Euler's equation.
- (k) Differentiate between Dynamic Programming Problem (DPP) and Linear Programming Problem (LPP).
- (l) Define functional of a curve.

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